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INFLUENCE OF SMALL SCALE YIELDING ON DYNAMIC FRACTURE.(U)  
MAY 80 A S KOBAYASHI, M RAMULU, B S KANG N00014-76-C-0060

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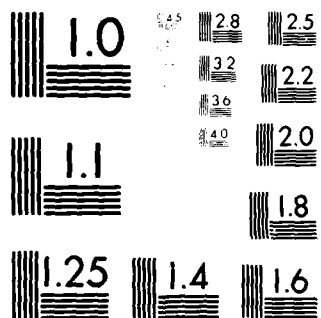
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Technical Report No. 38

**INFLUENCE OF SMALL-SCALE YIELDING ON DYNAMIC FRACTURE**

by

A.S. Kobayashi, M. Ramulu, and B.S.-J Kang

May 1980

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## SUMMARY

Dynamic fracture and crack-arrest responses of the well-discussed wedge-loaded rectangular, double cantilever beam (WL-RDCB) specimens machined from a 3.2 mm thick annealed polycarbonate sheet were studied by dynamic photoelasticity and dynamic finite element analysis. A small, but finite plastic yield zone surrounded the propagating crack which resulted in crack velocities, dynamic fracture toughness and crack arrest toughness lower than those observed previously in 6.4 mm thick polycarbonate fracture specimens.

## INTRODUCTION

Current experimental and numerical investigations in dynamic fracture involve extensive use of dynamic photoelasticity [1,2] dynamic caustics [3], dynamic finite difference analysis [4,5], and dynamic finite element analysis [6,7]. The results published in the above are based on the theory of elasto-dynamics and have evoked a controversy regarding the existence of a material property, i.e., a unique dynamic fracture toughness,  $K_{ID}$ , versus crack velocity relation,  $a$ , as a material property which governs dynamic crack propagation and arrest [1,2,6,8]. Despite this unresolved controversy on elastodynamic fracture, the increasing research efforts in this field should eventually lead to a phenomenological dynamic fracture criterion which can be used in either finite difference or finite element codes to predict crack propagation histories in actual structures. For example, recent numerical simulation of dynamic fracture in a thermally shocked structure [9] correlated well with experimental results [10] and undoubtedly such practical applications will increase as the controversies in elastodynamic fracture are resolved.

Unlike the efforts in elastodynamic fracture, little basic research in dynamic ductile fracture, particularly in the presence of large scale yielding has been conducted to date. Earlier investigations on dynamic ductile fracture, including

those of Kanninen et al [11], Hahn et al [12] and Ogasawara et al [13] as well as the recent papers by Koshiga et al [14] and Nora et al [15] involved phenomenological modelings of specific experimental observations. While these results are useful in predicting dynamic ductile fracture responses in specific structures, they fail to address the basic laws governing dynamic ductile fracture.

One major difficulty in dynamic ductile fracture research is the lack of suitable experimental technique with which the dynamic states of stress, strains, plastic yield zone, etc. can be measured directly for detailed scrutiny. In contrast, dynamic photoelasticity and dynamic caustics provide optical imaging from which the dynamic stress intensity,  $K_I^{dyn}$ , among others can be extracted for elastodynamic fracture studies. Lacking a pure experimental approach, one method which can be used is the combined experimental-numerical procedure for computing dynamic fracture parameters. In this procedure, experimental results such as crack position versus time in a fracturing specimen, is used to drive a crack in a finite element model of the fracture specimen. The numerical results, such as the equivalent dynamic stress intensity factor for elastic analysis, dynamic J-integral and crack opening angle, COA, among others can then be studied as candidate dynamic ductile fracture criteria. The soundness of this procedure when used in elastic analysis has been verified by one of the authors [2,16]. It was then used in a series of sensitivity studies on the influence of various dynamic fracture toughness,  $K_{ID}$ , versus crack velocity,  $\dot{a}$ , relations [17,18]. An obvious extension of this elastic procedure is its use in elasto-plastic analysis.

This paper reports some preliminary results obtained in the course of developing an experimental-numerical procedure for determining dynamic ductile fracture toughness which could be used to characterize the dynamic ductile fracture.

## EXPERIMENTAL ANALYSIS

The concurrent experimental analysis in this investigation consisted of

dynamic photoelasticity using thin, i.e., 3.2 mm thick, polycarbonate wedge-loaded, rectangular double cantilever beam (WL-RCB) specimens which is shown by Figure 1. The annealed polycarbonate, from which the specimens were machined, has a well-defined yield point of 44 MPa, flows under high stresses, and exhibits tensile instability with accompanying Lueder's bands. Under high strain rate loading, such as in the vicinity of a propagating crack tip, the strain-rate sensitive polycarbonate fractures in a cleavage mode without the large plastic zone ahead of the propagating crack tip. Such ductile to brittle transition in dynamic loading of polycarbonate is discussed in Reference [19]. Despite this cleavage fracture appearance, the dynamic photoelastic patterns in Figure 2(a) and 2(b) show that the propagating crack tip is preceded by a small yield zone of 1.2 mm and 0.4 mm diameters, respectively, and thus, represent dynamic fracture in the presence of small scale yielding. The elastic region surrounding this small yield zone also provides the elasto-dynamic state which can be used to extract apparent elastic fracture parameter for characterizing such dynamic ductile fracture. For example, the isochromatics form the standard loops from which apparent dynamic stress intensity factor can be extracted through the use of well-known elasto-dynamic near-field solutions [20]. Possible errors involved in characterizing the elasto-plastic dynamic field with such straight forward application of elastic analysis will be discussed later. The 16-spark gap Cranz-Shardin camera and the associated dynamic photoelastic systems used to record 16 discrete dynamic photoelastic patterns in the fracturing polycarbonate WL-RDCB specimen has been described in many previous papers and thus will not be repeated here.

In the as-received condition, the polycarbonate sheet exhibits considerable residual stress distribution and thus the sheets were annealed after rough cutting. This annealing, which caused some distortion and shrinkage, consisted of overnight heating at 160°C, followed by gradual cooling at the rate of 5°C per hour. The starter crack consisted of 0.4 mm wide edge crack approximately 25 mm length which

was machined and then chiseled to simulate a somewhat blunt crack tip. Static and dynamic stress-fringe constant and Poisson's ratio at various strain rates, all of which were determined previously [21], were used in data reductions. Static modulus of elasticity of  $E = 2.00$  GPa and the yield strength of 44 MPa were determined separately for this particular polycarbonate sheet.

#### CRACK TIP ISOCHROMATICS IN THE PRESENCE OF SMALL SCALE YIELDING

The influence of small scale yielding on the dynamic isochromatics surrounding the crack tip was studied by a static Dugdale strip yield model (DM) as shown in Figure 3. Since the Westergaard's stress function for a partially pressurized semi-infinite crack tip is known [22], the crack tip isochromatics,  $\tau_m$ , for a stationary crack with a Dugdale strip yield of length  $r_y$ , can be expressed as

$$\tau_m = \frac{1}{2}[(\sigma_{xx} - \sigma_{yy})^2 + 4\tau_{xy}^2]^{\frac{1}{2}} \quad (1a)$$

where

$$\sigma_{xx} - \sigma_{yy} = K_I \frac{\sin \theta_{DM}}{\sqrt{2\pi r_{DM}}} \frac{\frac{r_y}{r_{DM}} \sin \frac{\theta_{DM}}{2} + \sin \frac{3\theta_{DM}}{2}}{\left(\frac{r_y}{r_{DM}}\right)^2 + 1 + 2 \frac{r_y}{r_{DM}} \cos \theta_{DM}} \quad (1b)$$

$$2\tau_{xy} = -K_I \frac{\sin \theta_{DM}}{2\pi r_{DM}} \frac{\frac{r_y}{r_{DM}} \cos \frac{\theta_{DM}}{2} + \cos \frac{3\theta_{DM}}{2}}{\left(\frac{r_y}{r_{DM}}\right)^2 + 1 + 2 \frac{r_y}{r_{DM}} \cos \theta_{DM}} \quad (1c)$$

where  $r_{DM}$  and  $\theta_{DM}$  are the polar coordinates with origin at the DM crack tip in Figure 3. The stress intensity factor,  $K_I$ , corresponds to the negative of the stress intensity factor at the DM crack tip without the Dugdale strip yield zone. From the equality, the length of the DM zone becomes

$$r_y = \frac{\pi}{8} \left( \frac{K_I}{\sigma_y} \right)^2 \quad (2)$$

where  $\sigma_y$  is the yield strength of the material.

The resultant crack tip isochromatics in the presence of a DM zone can be obtained numerically for the highly loaded crack tip at the onset of crack propagation. For estimated stress intensity factor of  $K_I = 2.44 \text{ MPa}\sqrt{\text{m}}$ , yield strength of  $\sigma_y = 44 \text{ MPa}$  and an isochromatic fringe order of  $7\text{-}1/2$  or  $\tau_{\text{max}} = 84.8 \text{ MPa}$  in the 3.2 mm WL-RDCB specimen. The DM strip yield length is  $r_y = 1.3 \text{ mm}$ . Figure 4 shows the estimated crack tip isochromatics with the DM zone and the experimentally observed isochromatics of Figure 2(a). The significant difference between the estimated and experimental isochromatics indicate the amount of plasticity correction necessary to increase the elastic  $K_I$  in the presence of small scale yielding.

The procedure then for estimating the apparent stress intensity factor from the isochromatics in the presence of small scale yielding is to first estimate the location of the far end of the crack tip yield zone or the DM crack tip location in the photoelastic pattern. An overdeterministic least square method [23] is then used to fit at the DM crack tip a two parameter, elastic crack tip stress field to the experimentally recorded isochromatics. Using the elastic stress intensity factor thus computed, the DM strip yield length  $r_y$  is determined by equation (2) and the estimated isochromatics is reconstructed numerically by the use of equation (1). Should the computed  $r_y$  be substantially different from the measured  $r_y$ , then  $r_y$  must be remeasured and the above numerical procedure is repeated. Fortunately, such repeated measurement was not necessary in the test analyzed for this paper. The ratio of the maximum radial distances,  $r_M$  and  $r_{DM}$  in Figure 4, is the plasticity correction factor. This procedure must be repeated until the succeeding plasticity correction factor approaches unity. However, in view of the



approximate nature of the entire procedure, this iteration procedure was not programmed into this data reduction scheme.

The above procedure is based on static crack tip yielding and obviously must be modified for dynamic analysis. It, however, provides a first order estimate of the plasticity correction involved in deducing the apparent dynamic stress intensity factor from the dynamic isochromatics in the presence of small scale yielding.

#### DYNAMIC FINITE ELEMENT ANALYSIS

The dynamic finite element algorithm used in this study differs with that presented two years ago [24]. The new fracture package [2] includes a mechanism for gradual release in crack tip nodal force as well as an iteration routine to assure agreement between the prescribed and computed crack tip nodal forces in this explicit code. Figure 1 shows the finite element breakdown used in this plane stress analysis which is considered more appropriate for these thin fracture specimens, despite the cleavage fracture surfaces. The dynamic finite element code was executed in its elastic-plastic mode. The coarseness of finite element breakdown, i.e., 3.2 mm square in comparison to the observed maximum plastic yield zone of 1 mm, however, forced the actual computation into its elastic mode except for the initial 1-2 microseconds in crack propagation time. As a result, the dynamic stress intensity factor,  $K_I^{\text{dyn}}$ , was computed elastically using the dissipated energy at the released node with Freund's equation [25].

#### RESULTS OF DYNAMIC PHOTOELASTICITY

A total of seven dynamic photoelastic tests were conducted. Figure 2 shows two typical dynamic photoelastic patterns of a fracturing polycarbonate WL-RDCB specimen. These dynamic photoelastic patterns show crack tip shadow patterns which are believed to be caustics [3] generated by the large plastic strains in the con-

finer plastic region ahead of the propagating crack tip. The size of such a plastic zone ranges from  $r_y = 1.3 \text{ mm}$  to  $0.04 \text{ mm}$ . Minor distortions of the otherwise elastic isochromatics in the vicinity of this plastic region is also noted.

Apparent dynamic stress intensity factor,  $K_I^{\text{dyn}}$ , was computed by using the data reduction procedure described previously. Figure 5 shows the apparent dynamic fracture toughness, which were obtained by this procedure, during dynamic fracture and crack arrest in a polycarbonate WL-DCB specimen. The general variation of these experimental results differs slightly with those obtained by others [3,7]. The apparent dynamic fracture toughness continues to decrease in the former while distinct regions of constant  $K_{ID}$  after crack propagation were observed in the latter. The crack initiation stress intensity factor of  $K_{IQ} = 7.37 \text{ MPa}\sqrt{\text{m}}$  is more than twice of the pop-in fracture toughness of  $K_{IC} = 3.4 \text{ MPa}\sqrt{\text{m}}$  measured previously [21]. The measured apparent crack arrest fracture toughness of  $K_{Ia} = 1.0 \text{ MPa m}$ , however, is considerably lower than this pop-in fracture toughness and lower than the  $K_{Ia} = 1.4 \text{ MPa}\sqrt{\text{m}}$  reported for the 6.4 mm polycarbonate fracture specimens [2].

Also shown in Figure 5 is the crack velocity change with crack extension in this WL-RDCB specimen. This crack velocity history was duplicated in the other six specimens and are similar in shape to those reported by others [3,26] but the terminal velocity is lower than that in Reference [2].

#### RESULTS OF DYNAMIC FINITE ELEMENT ANALYSIS

Figure 5 shows the calculated dynamic stress intensity factor obtained through elasto-dynamic finite element analysis. As mentioned previously, the finite element analysis was executed in its elastic-plastic mode, but elastic analysis prevailed except for the initial 1-2 microseconds of crack propagation. Agreements between calculated dynamic stress intensity factors and the measured

dynamic fracture toughness during crack propagation history are apparent. The precipitous drop in calculated dynamic stress intensity factor at the initial phase of crack propagation can be in part attributed to the infinite plate syndrome discussed by Perl [27]. It was also found that this precipitous drop in dynamic stress intensity factor could be moderated by assigning a gradually increasing crack velocity during the first 30-50 microseconds of crack propagation following Reference [27]. Recent experimental results [20,28,29], however, show that the crack velocity of a blunt starter crack immediately reaches the terminal velocity upon propagation and does not gradually approach the terminal velocity as postulated in Reference [27] during this crucial initial period of crack propagation. These experimental evidences thus precluded adjustments of crack velocity to reduce the precipitous drop in  $K_I^{dyn}$ .

Figure 6 shows the energy partitions during crack propagation in the WL-RDCB specimens discussed previously. Although the dissipated plastic energy at the plastic yield zone was not computed in this coarse finite element model, the decreasing total energy in Figure 6 indicated qualitatively, the small plastic energy dissipated in the fracture process of polycarbonate WL-RDCB specimen.

#### CONCLUSIONS

1. Small-scale yielding at the propagating crack tip does change the shape of the crack-tip dynamic isochromatics.
2. Crack velocity, dynamic fracture toughness and crack arrest toughness are lower in the presence of small-scale yielding at the propagating crack tip.
3. Dynamic stress intensity factor obtained by elasto-dynamic finite element analysis are in good agreement with the apparent dynamic fracture toughness obtained through an elasto-plastic data reduction of the dynamic isochromatics in the presence of small scale yielding. Elasto-plastic dynamic finite element analysis, does not appear necessary for such dynamic fracture problems.

4. The decreasing total energy indicate the influence of dissipated plastic energy in the presence of a small plastic zone.

#### ACKNOWLEDGEMENTS

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TOTAL NUMBER OF ELEMENTS 175  
TOTAL NUMBER OF NODES 208

ALL DIMENSIONS IN mm

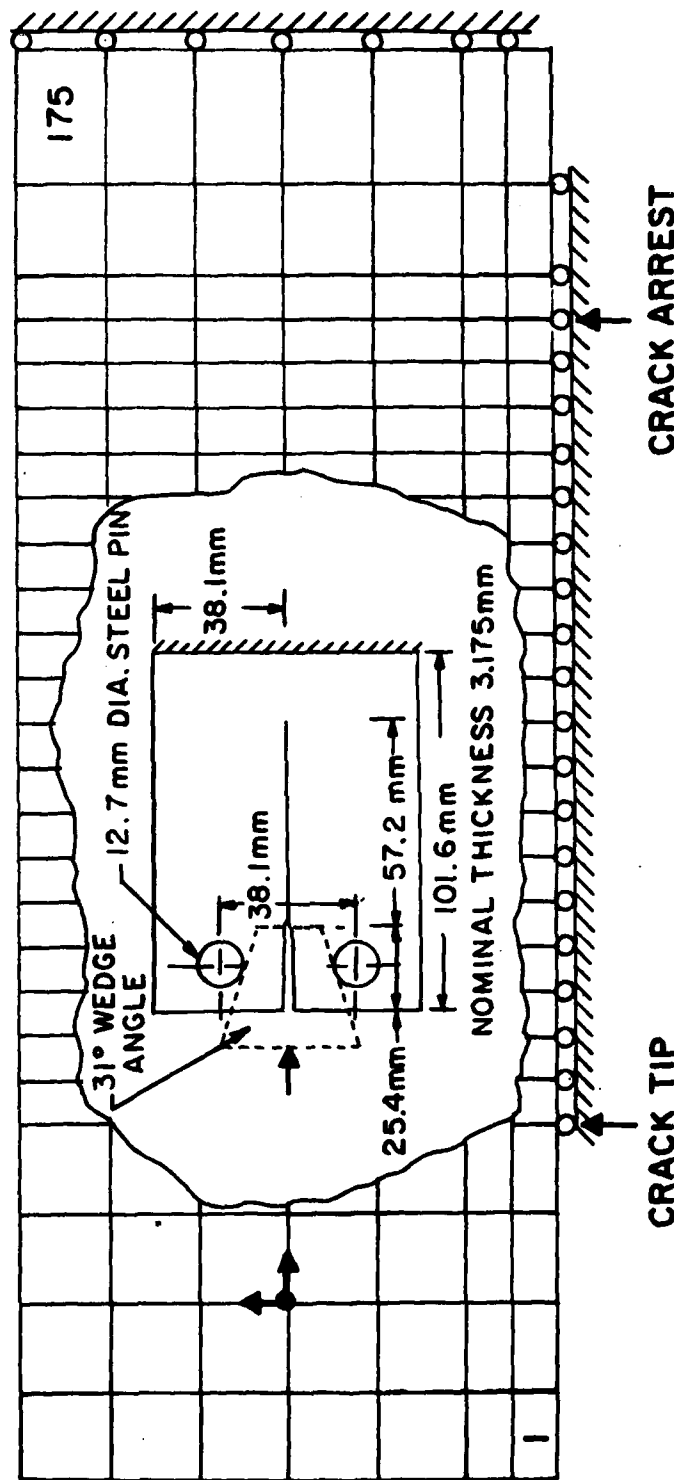


FIGURE 1 . FINITE ELEMENT BREAKDOWN OF WL - DCB SPECIMEN .



(a) 1ST FRAME 7  $\mu$  SECONDS



(b) 7TH FRAME 71  $\mu$  SECONDS

FIGURE 2. TYPICAL DYNAMIC PHOTOELASTIC PATTERNS IN POLYCARBONATE WL-DCB  
SPECIMEN NO. K031380-P.



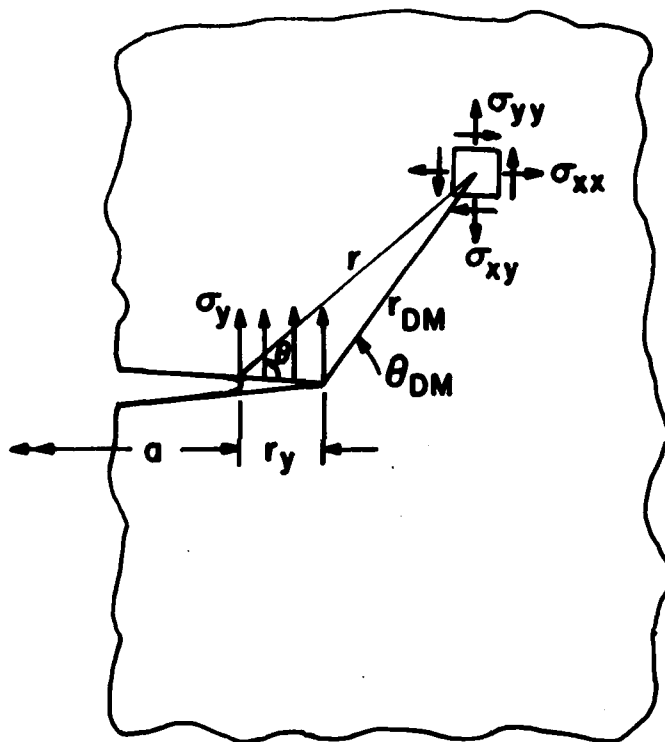


FIGURE 3. DUGDALE STRIP YIELD ZONE AT THE CRACK TIP OF A SEMI-INFINITE CRACK.

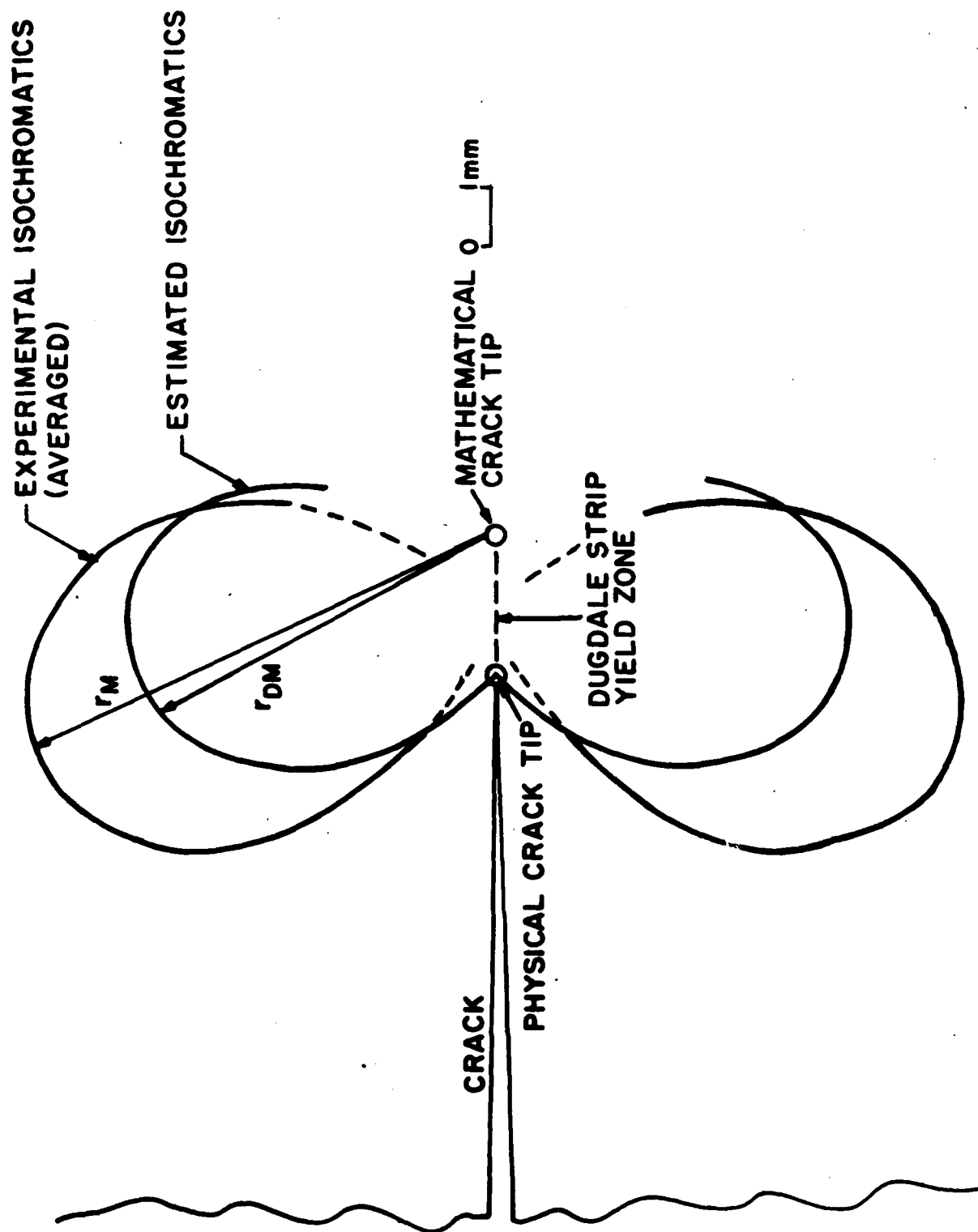


FIGURE 4. EXPERIMENTAL AND ESTIMATED ISOCHROMATICS.

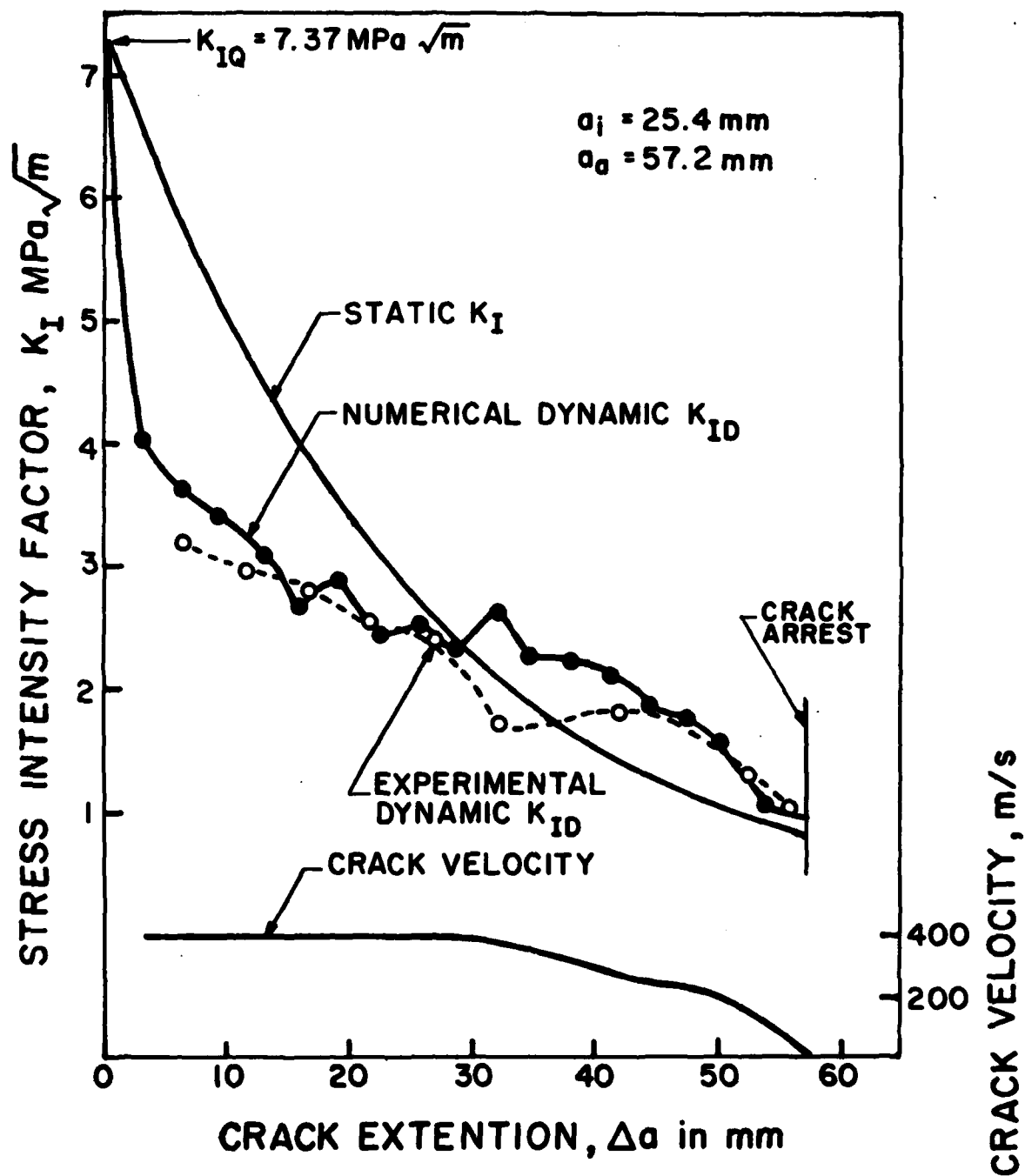


FIGURE 5. STRESS INTENSITY FACTORS OF A FRACTURING POLYCARBONATE WL-DCB SPECIMEN NO. K031380-P.

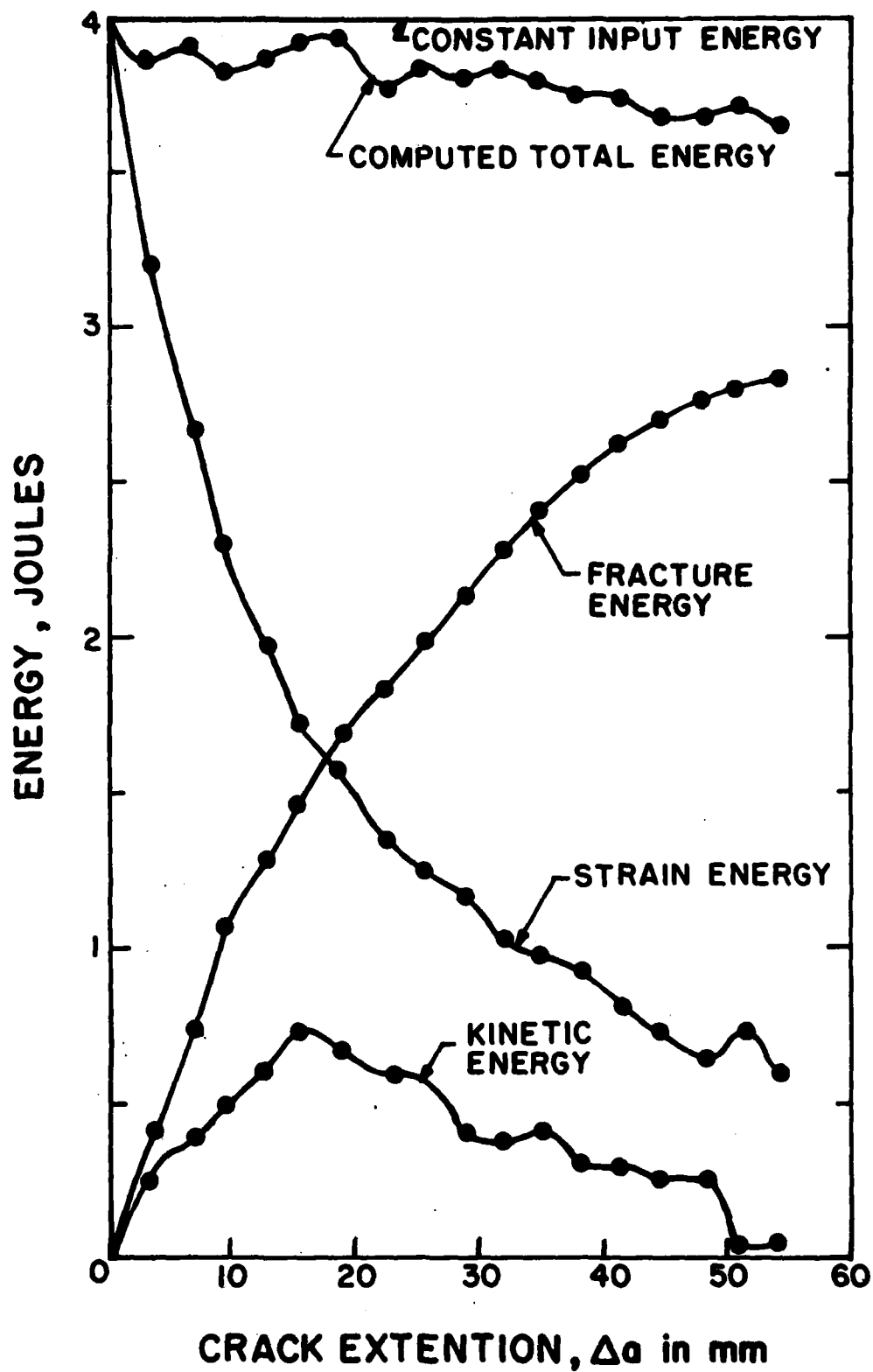


FIGURE 6. ENERGY OF A FRACTURING POLYCARBONATE WL-DCB SPECIMEN NO.K031380-P.

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